

Keysight Technologies

# Evaluation of the Performance of a State of the Art Digital Multimeter

White Paper

## Abstract

The introduction of a state of the art digital multimeter presents a real challenge to the standards lab to provide external verification of its performance. The advent of internal standards and automatic internal calibration of all the DMM's functions from those standards pits the calibration expert, his methods and equipment against an effective machine capable of extreme levels of accuracy. Conventional metrology methods if used very carefully are capable of verifying the DMM's performance but there is very little room for error. The mindset of the metrologist must change because sources of error which may have been negligible in the past are now significant.

The main purpose of this paper is to describe some methods which have been found adequate to verify the performance of a very accurate automatically calibrated DMM, the HP 3458A. The verification processes have been automated as much as is practical. With well characterized processes in place it is possible to develop history on the DMM's performance. Data have been obtained on a number of HP 3458A's which indicate that the autocalibration processes work extremely well and that the instrument definitely has the capability to perform standards lab measurements at very high levels of accuracy. Also included is a description of use of a 10 volt Josephson junction array to measure linearity of the A/D converter of the 3458A, and some results of these measurements.

Verification of A/D converter linearity is imperative, since the A/D in the 3458A is used to provide all the ratios needed for the internal autocalibration processes.



Unlocking Measurement Insights

## Introduction

The HP 3458A DMM represents a new generation of ultra-high performance digital multimeters. It contains internal standards, circuitry and microprocessor power which enable internal self-calibration and produce performance that rivals some of the better standards lab capabilities available today. In order to establish confidence in the performance of such a “box full of automated metrology,” it is necessary to assess its performance on each function and range by comparison with external standards. While many of the methods described in this paper can be applied to evaluation of any precision DMM, some of the procedures are specifically tailored for the HP 3458A DMM.

The basis of autocalibration is fairly straightforward. By comparing measurements of well known external standards to measurements of its internal standards, the DMM determines the values of its internal standards. In the case of the HP 3458A, the only internal standards are a single value each for DC voltage and resistance. These standards are relatively insensitive to ambient conditions and have excellent time stability. The instrument then uses these internal standards in a number of built-in autocalibration processes to establish its accuracy for all ranges and functions. It actually performs over a quarter million measurements in the process. Its overall accuracy and stability are then dependent upon several factors which include:

- Accuracy of the external calibration standards
- Stability of its internal reference standards
- Its ability to compare the above standards
- Its ability to transfer these standards to other ranges and functions
- Overall quality of its internal calibration processes
- Stability of its measurement circuitry between internal calibrations

These factors can be logically divided into two groups. They are:

- Reference standards, which primarily affect long-term performance (> 24 hours)
- Autocalibration processes and measurement circuitry, which primarily affect short-term performance (< = 24 hours)

These long and short term effects can be studied separately. This paper deals mainly with the short-term portion. Long-term assessment of the performance of reference standards is a separate topic.

Following is a very brief summary of the steps involved in calibrating the 3458A prior to evaluation of its performance. First a four-terminal short circuit is applied to the input terminals and the appropriate calibration command is executed. Next a precisely known DC voltage source (nominal 10 V) and 10 k $\Omega$  resistor are successively connected, their values entered into the 3458A and the appropriate calibration commands are given. It is important that OCOMP be turned on prior to connecting the 10 k $\Omega$  standard if ultimate accuracy is desired and the 3458A will be used with OCOMP on when measuring resistance. The instrument performs several internal self-adjustment steps after each command. Its absolute accuracy for all parameters it measures will depend upon the accuracy of the values which are entered for the standards. Reference 6 contains detailed information about the internal self-adjustment processes.

## Introduction (Continued)

This paper will describe some more or less conventional metrology methods which have been developed to determine the performance, in particular to verify the 24-hour specifications of this very accurate DMM. In general, the simple fundamental methods seemed to produce the best results. There are often several valid ways to achieve the same objective in metrology, and the methods chosen are somewhat dictated by available standards and equipment. The methods presented here may not be practical in every laboratory but they should at least provide ideas for alternative methods.

The verification of the various functions and ranges is divided into several areas: DC voltage, resistance, DC current, AC voltage, and AC current.

A real advantage provided by an autocalibrated instrument is that when its results agree very closely with carefully derived and highly accurate external stimuli, some confidence in the results is gained by the agreement. As these procedures were being developed, the instrument was capable of pointing out that some of the external metrology tried was in need of some improvement before it would be adequate to verify 3458A performance.

## Methods Used for Verification of Performance

### DC voltage

A prime requirement for evaluating DC voltage performance at the accuracy level required is that the uncertainties in the metrology process used be kept at an absolute minimum. All DC voltage standards used should be tied as closely as possible to the 10 V calibration standard. The 24 hour DC voltage specifications for the 3458A are 0.5 ppm at 10 V, 2 ppm at 1 V, and 3 ppm at 100 mV. Using standard resistors in a 25 °C oil bath, several very simple dividers were set up and evaluated and found to produce adequate results. These resistors are periodically calibrated to absolute values starting from a Thomas one ohm primary standard. Ratio techniques are used to scale from one decade to the next. A closure check is also made at the 10 k $\Omega$  value against a 10 k $\Omega$  primary standard. Agreement is normally within a few tenths of a ppm. Kelvin Varley dividers were tried and even after externally evaluating their errors they were found to be not adequate for the task.

See Figure 1 for the setup used to evaluate the lower three voltage ranges. First, the offset errors of the DMM are evaluated by connecting a low thermal short to its input and taking readings on each range. An accurately known voltage which is nearly full scale is then applied to the input and more readings taken (both forward and reverse). In the case of the 10 V range, the applied voltage is the same 10 V zener reference which was used to calibrate the DMM. The 1 V and 100 mV range gain errors are checked by connecting the oil bath resistive dividers between the 10 V zener reference output and the DMM input. The simplicity of these dividers outweighs the fact that their outputs are not exact cardinal values. Corrections must be applied for divider loading effects on the zener reference output as well as the drop through the connecting leads, even though they amount to only a few tenths of a PPM.

Any thermal emfs or other offsets in the divider network must also be dealt with. This is accomplished by first shorting the divider input leads and taking a DMM reading. In the setup used, it was found that the low voltage side of the divider achieves adequate thermal stability such that changes in thermal emfs during the measurement period are not large enough to require a time dependent model to cancel them out. The leads from the oil bath divider to the DMM are not disturbed during the measurement sequence. Connections to the resistors are made using mercury wetted connections inside the oil bath. It is imperative that careful attention be paid to these minute sources of error, because they can easily be large enough to make the 3458A appear to not meet its specifications if they are not properly handled.

Reversals for evaluating DMM negative reading performance are done with the divider input so that the effects of thermal emfs caused by the reversal process are relative to 10 V and are minimal. The divider uncertainties are about 0.6 ppm of output for 1 V and about 1 ppm of output for 100 mV. The burden for accuracy of the low voltages is placed squarely on the resistor ratios. Another possible candidate for establishing these accurate dividers is a series-parallel self calibrating ratio method, but it was not used because the simpler methods described above worked well enough.

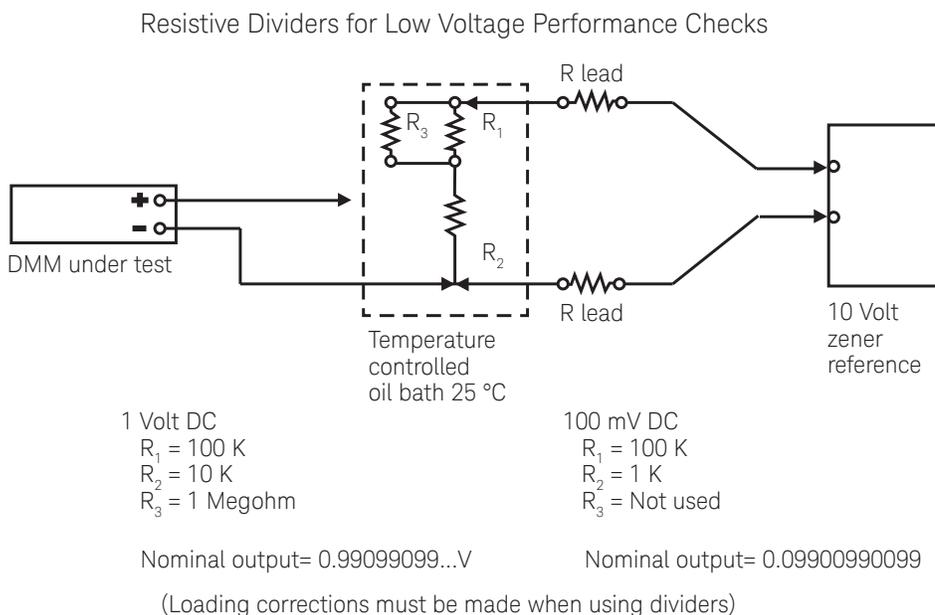


Figure 1.



## Methods Used for Verification of Performance (Continued)

### Resistance

There are nine resistance ranges, and verification of the lower seven of these involves use of the same standard resistors in the oil bath. The resistors we use are calibrated with the mercury wetted connection resistance included in the assigned value, (except one ohm, which is connected as a true four-terminal device) and they are connected the same way for all applications described here. The resistance of each mercury wetted contact is approximately  $10\ \mu\Omega$  and its repeatability is on the order of a micro ohm. The 3458A is used with four-wire connections up to the heavy copper bars of the oil bath. In evaluating the resistance performance of the 3458A, the offset compensated four-wire ohms mode (OCOMP) must be selected for all ranges  $10\ \text{k}\Omega$  and below. OCOMP removes the effects of thermal emf's in the measurement circuit by taking readings both with and without the DMM's internal current source turned on and using the difference between the two readings to negate the effect of thermal emf's in the measurement leads.

A digression is in order at this point to provide some additional information regarding OCOMP which can affect the results it produces. As with many such beneficial features, there are cases where improper use of OCOMP can introduce a different kind of error. This error is related to the fact that the times between the current on and current off measurements must allow sufficient relaxation of the measurement circuit. This relaxation time can be a simple RC time constant or it can be tied to a much more insidious and slower effect called dielectric absorption (DA). DA effects can be caused by any dielectrics in the measurement circuit, including insulation on the leads. The 3458A has a programmable delay which has default values depending upon range. The  $100\ \text{k}\Omega$  range is where DA problems are most likely to occur. The OCOMP feature is automatically disabled for ranges above  $100\ \text{k}\Omega$ . The relative DA problem caused by various dielectric materials can be observed by connecting a  $100\ \text{k}\Omega$  resistor in four-wire mode (using twisted pairs) with OCOMP ON and experimenting with different wire insulation materials and delays. Using the default delay in the 3458A, the difference between PVC and PTFE insulated leads about 24" long is very noticeable (provided that DA in other dielectrics in the measurement circuit is not swamping out the effect of the leads). Normally, programming a sufficient delay will eliminate such problems. All of the above discussion of OCOMP also applies to use of the  $10\ \text{k}\Omega$  external standard which is used to calibrate the 3458A.

Relative to the  $10\ \text{k}\Omega$  standard used to calibrate the DMM, achievable uncertainties for the oil bath resistors are 1 ppm or less for values from  $10\ \Omega$  through  $100\ \text{k}\Omega$ . These widen to about 2 ppm at  $1\ \text{m}\Omega$  and about 5 ppm at  $10\ \text{m}\Omega$ . When compared to the 24 hour specs for the DMM, these provide usable if not comfortable accuracy ratios. Fortunately the ranges where the specs are tightest,  $1\ \text{k}\Omega$ ,  $10\ \text{k}\Omega$  and  $100\ \text{k}\Omega$ , involve either direct measurement of the  $10\ \text{k}\Omega$  calibration standard or a single decade ratio from it. The 24-hour spec for these three ranges is 2.2 ppm. Again, the DMM has been found to be an excellent cross-check on the metrologist and his methods.

## Methods Used for Verification of Performance (Continued)

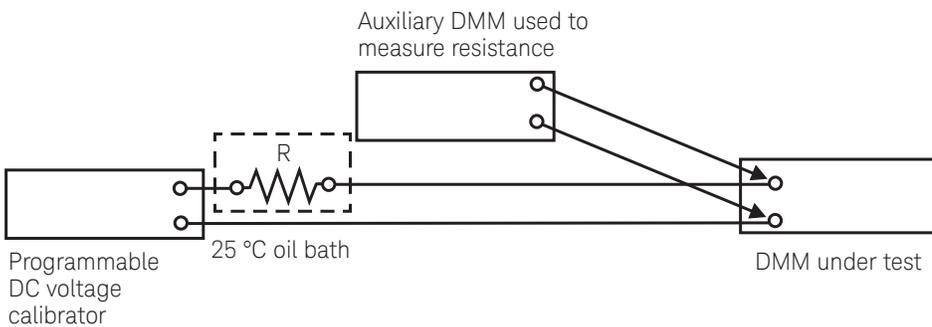
### DC current

Verification of the 100 nA, 1  $\mu$ A and 10  $\mu$ A current ranges could possibly be done directly with some sort of current source, but an indirect method was chosen which allows use of commonly available standards. The scheme used amounts to measuring the input resistance of the DMM being evaluated, then connecting a voltage source and series standard resistor to the DMM inputs and applying a calculated voltage to develop the desired current. See Figure 3. The measurement of the DMM input resistance must be done carefully, since protection devices inside the DMM can be turned on if too large a voltage is developed across the input terminals. Since the protection devices are nonlinear, errors will result if they are activated. Also, the 3458A being measured must be locked onto the proper current range.

Recommended measurement currents for determining input resistance are shown below as well as the correct resistance range to use if another 3458A is used to make the measurements.

DUT current range	Applied current	Auxiliary 3458A resistance range
100 nA range	0.5 $\mu$ A	10 m $\Omega$
1 $\mu$ A range	5 $\mu$ A	1 m $\Omega$
10 $\mu$ A range	50 $\mu$ A	100 k $\Omega$

100 nA, 1  $\mu$ A and 10  $\mu$ A Current Verification



100  $\mu$ A thru 1A Current Verification

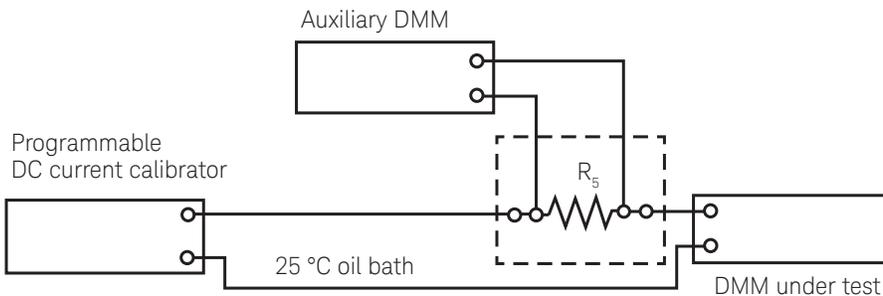


Figure 3 and 4.

## Methods Used for Verification of Performance (Continued)

### DC current (Continued)

For the higher current ranges, the evaluation consists of connecting a current source in series with a well known standard resistor and measuring the voltage across the resistor with another carefully calibrated voltmeter. This is shown in Figure 4. The oil bath resistance standards are used here also. The following table shows the resistors used and indicates the accuracies needed. The voltmeter must be accurate to within a few microvolts at 1 and 0.1 V, and must have an input resistance of at least 10 E10  $\Omega$ . A second 3458A could be used for this measurement.

Resistor uncertainties of a few ppm for 100  $\Omega$  through 10 k $\Omega$  are adequate and requirements are less severe for the 10 and 0.1  $\Omega$  values. These methods for verification of both low and high currents have produced excellent agreement with the 3458A's internal self-adjustments.

Range	Resistor	Nominal resulting voltage	24-hr spec
100 $\mu$ A	10 k $\Omega$	1 V	16 ppm
1 mA	1 k	1 V	14 ppm
10 mA	100 $\Omega$	1 V	14 ppm
100 mA	10 $\Omega$	1 V	29 ppm
1 A	0.1 $\Omega$	0.1 V	110 ppm

## Methods Used for Verification of Performance (Continued)

### AC voltage

Since the most accurate mode of AC voltage operation for the 3458A is the SYNC sampling mode, the following discussion is aimed at checking that mode. There are several setup parameters which must be input to the 3458A in order to set it up for maximum accuracy. These are: SETACV SYNC, RES=.001, ACBAND 10, 2E6, LFILTER ON. The 3458A manual explains these parameters. First an overview of the methods used to verify AC voltage performance will be presented. Refer to Figure 5 for a block diagram of the process.

Verification of a large portion of the DMM's AC voltage performance can be accomplished by careful application of classical thermal AC/DC transfer techniques. For checking the 100 mV range, other methods employing carefully calibrated dividers driven by known input voltages are used. For frequencies above 1 MHz, a 50  $\Omega$  system is used which has been calibrated and corrected for flatness. This system is referenced by comparison with established voltages at 100 kHz.

The process chosen to perform the thermal transfer measurements starts with a set of primary standard single range thermal voltage converters (TVCs) with range resistors. This set of TVCs is periodically calibrated by NIST and is used to periodically determine the errors of a commercially available automatic thermal transfer standard (ATS) which is controlled by a computer. The primary standard TVC is connected to the ATS by a tee which is driven at its center by a programmable AC/DC voltage source using remote sensing. The AC accuracy of the source is immaterial, however, its DC voltage output is used as the reference for the primary standard TVC AC/DC transfer, and must be reasonably well calibrated.

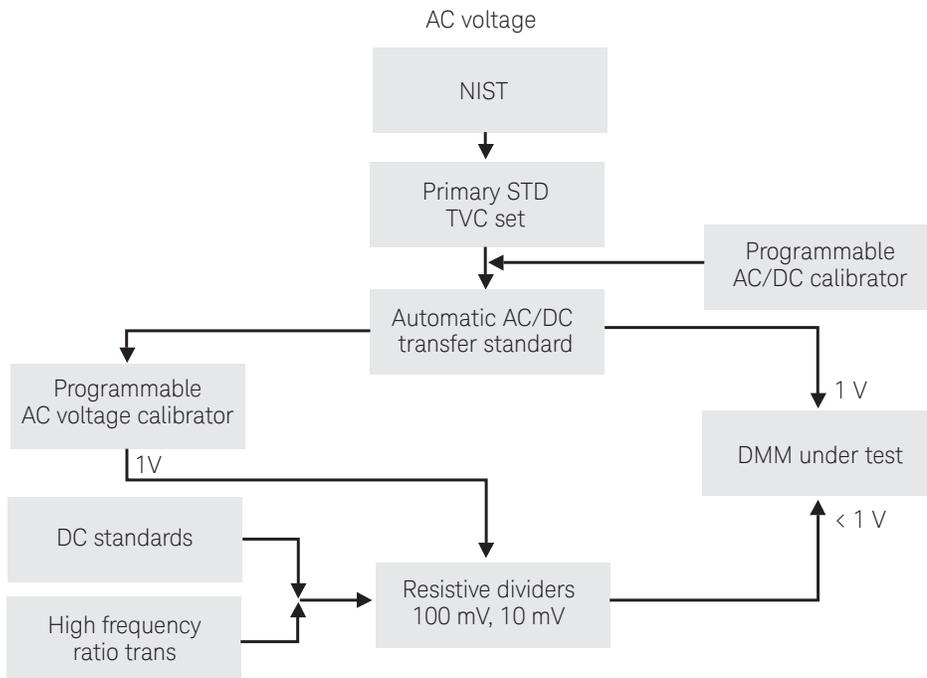


Figure 5.

## Methods Used for Verification of Performance (Continued)

The output of the primary standard TVC is read by a programmable DMM. The normal drift canceling DC-, AC, DC+ reversal process is used for the primary TVC. See reference 4 for a discussion of the importance of using a drift canceling algorithm. Special algorithms have been implemented in the controller software to enhance the performance of the ATS. In addition, some hardware modifications were made to the ATS to obtain lower uncertainties. The whole process is automated, and Figure 6a shows how the devices are connected.

A matrix of error data for the ATS is thus generated and stored in a file. These errors represent the error in its response versus the actual input voltage, expressed as percent or ppm. It is necessary to generate data for each voltage and most frequencies to be used, since interpolation can lead to amplitude dependent errors. These errors arise from the fact that the turnover of the thermal converter in the ATS will, in general, be amplitude dependent and it does not employ DC reversal. The periodic evaluation of the ATS's errors has proven adequate to detect and correct for changes that may occur in its response. There are many potential causes of changes in response including internal drifts and changes in tee contact resistance. Some of these potential sources of error can be evaluated by application of a well known DC voltage to the ATS via the tee.

The ATS is then used to determine the errors of the DMM being evaluated. The DMM is connected to one leg of the tee using a 6" long twisted pair with a programmable AC source driving the center of the tee. See Figure 6b. Readings are made with the ATS and the DMM. Then, using the data in the error matrix for the ATS, the DMM errors are calculated. This process is also automated. The error introduced by the 6" twisted pair is of the order of 10 ppm at 100 kHz and less at lower frequencies.

Development of intelligent algorithms and software to accomplish all the steps in this scheme required a lot of time and effort, but has resulted in a system which has the capability to not only evaluate the DMM, but can also be used to determine the errors of an AC calibrator. Of course this method is subject to the usual limitations of thermal devices regarding lack of low voltage capability and speed among others. Having an automated process for verification of the AC voltage performance of the DMM is mandatory. Repetitive performance of these tedious procedures manually leads to extreme operator fatigue and measurement errors.

The process used to evaluate the performance of the 100 mV range of the DMM uses a calibrated AC voltage source at 1 V to drive a resistive divider (using remote sensing inside the divider). The errors in the source are periodically evaluated using the ATS. The divider used is a 200  $\Omega$  per volt device which presents the same load to the source as the ATS. The output impedance of this divider is high enough to cause a significant error when connected to the 1 m $\Omega$  input resistance of the 3458A in ACV SYNC mode, so a mathematical correction must be made. The divider ratio is determined by two methods, DC voltage ratio (both polarities) and by comparison with a standard inductive divider (ratio transformer). This divider ratio data is used at frequencies up to 1 kHz. The same divider is also used at frequencies up to 1 MHz, although the uncertainties required to verify the specs of the 3458A are considerably larger. A second set of ratio data for the divider is generated at 20 kHz using a six decade high frequency ratio transformer. The process of 3458A verification from the divider is also automated. See Figure 6c. The tightest specs for the 3458A occur between 40 Hz and 1 kHz, at 100 ppm.

## Methods Used for Verification of Performance (Continued)

An estimate of the overall uncertainty for the AC voltage verification process described above, using three sigma for the random sources of error, is about 40 ppm in the audio frequency range. A detailed discussion of uncertainties of these processes for other voltages and frequencies versus 3458A specs would be too lengthy for this paper. Data taken on 3458A DMMs are routinely well within the 24-hour specs for the instrument. The data contained in [5] indicate that the measurement process described above is capable of state of the art performance.

### Calibration Setup to Determine Errors in Automatic AC/DC Transfer STD

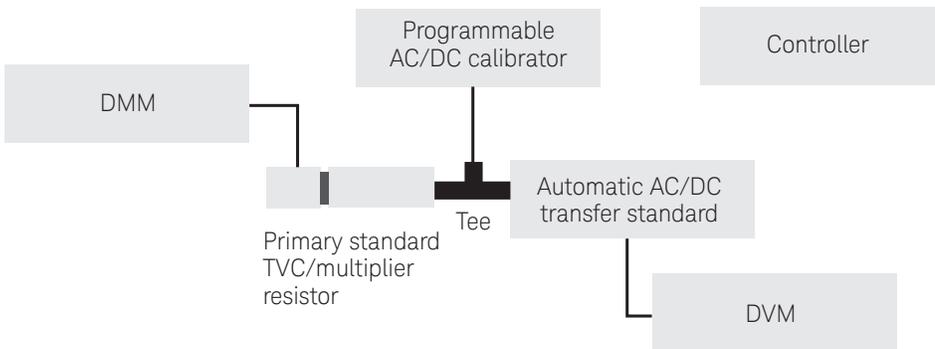


Figure 6a.

### Setup for Verification of ACV DMM Performance ( $\geq 1$ V RMS)

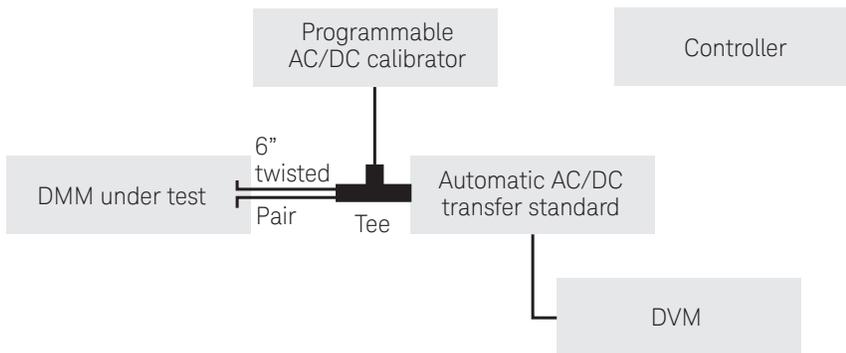


Figure 6b.

### Setup for Verification of ACV $< 1$ V RMS

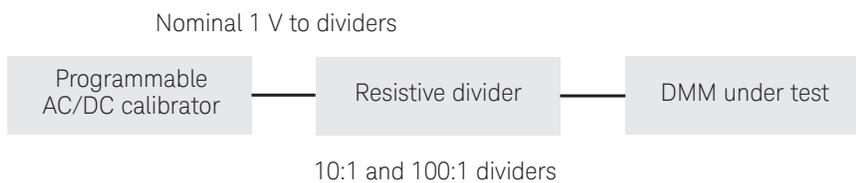


Figure 6c.

## Methods Used for Verification of Performance (Continued)

### AC current verification

Verification of AC current performance of the 3458A can be performed using a programmable AC voltage and current calibrator. The errors in the calibrator are periodically determined by measurements made with a set of primary standard current shunts and a thermal voltage converter calibrated by NIST. In order to verify the low current ranges (<10 mA) it was necessary to build a set of shunts using low reactance resistors and use ratio methods to determine the errors in the calibrator's output. Voltages across the shunts are measured with a DVM, and the loading effect of the DVM's input impedance is significant. Appropriate corrections must be made.

After the errors in the current calibrator are determined, it is then connected to the input of the DMM under test and readings are taken. This process is also automated, although checking the current errors of the calibrator is only semiautomated.

### Results

After a number of HP 3458A's had been evaluated using the processes described above, it seemed natural to put all 87 measurements for a number of instruments into a computer spreadsheet and do some analysis. Probably one of the better formats to see how well the instruments perform is to look at a histogram for each parameter. As a result, 87 histograms were generated, each containing the data for 41 separate HP 3458A's. Originally, the spreadsheet contained data for 57 instruments, but there were some known firmware problems in the early ones. The data set was cut down to exclude these known problems, and produce a valid sample of normal production units.

Each of the 87 histograms is plotted such that the edges of the histogram represent approximately the 24-hour specifications of the 3458A. Figures 7 through 13 are examples of these histograms. Space precludes including all of them, but none of the results were beyond the specification limits for any of the parameters.

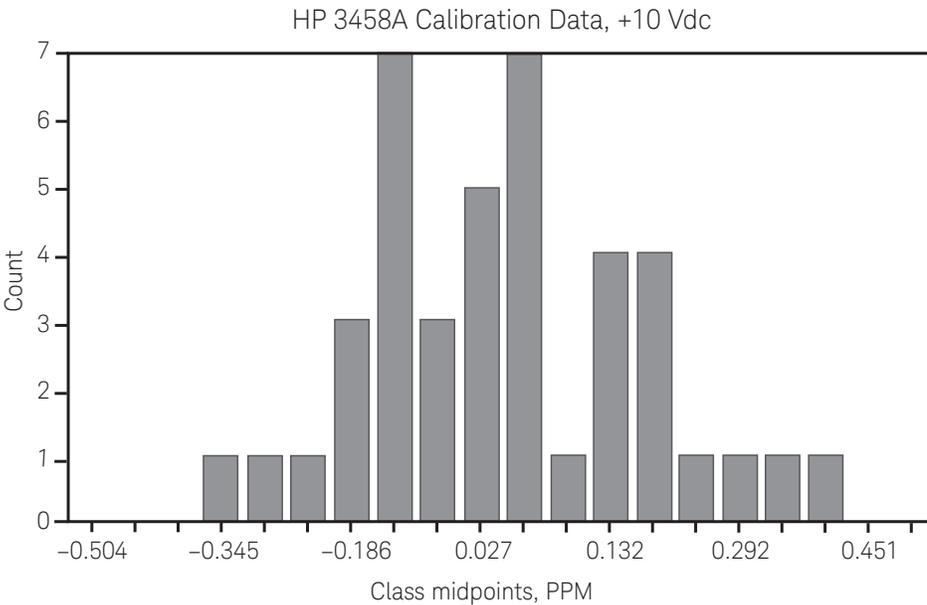


Figure 7.

## Methods Used for Verification of Performance (Continued)

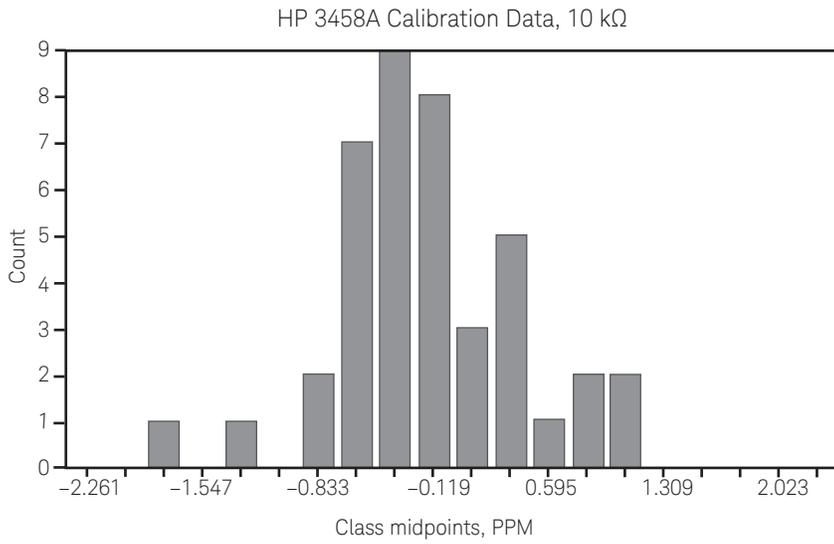


Figure 8.

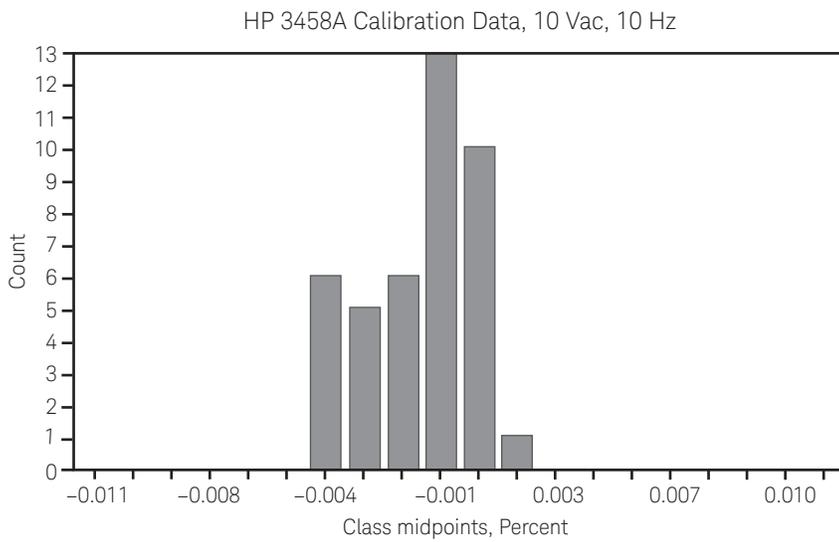


Figure 9.

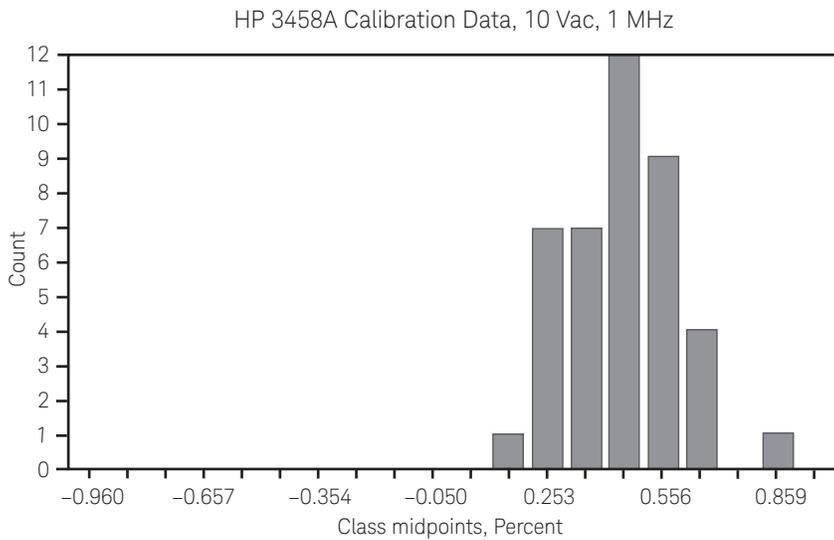


Figure 10.

## Methods Used for Verification of Performance (Continued)

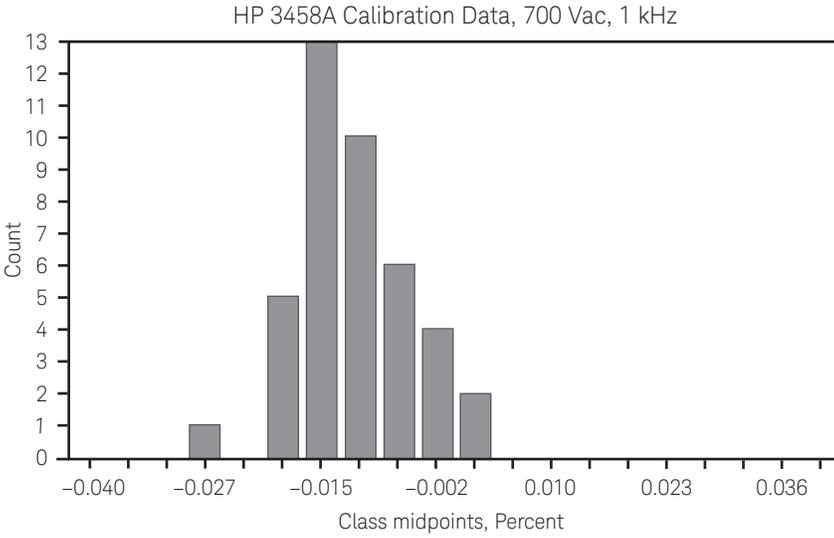


Figure 11.

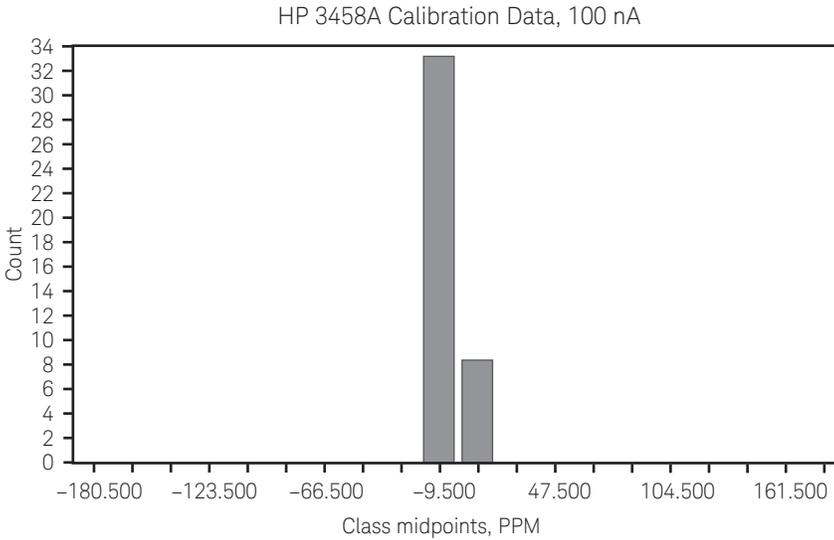


Figure 12.

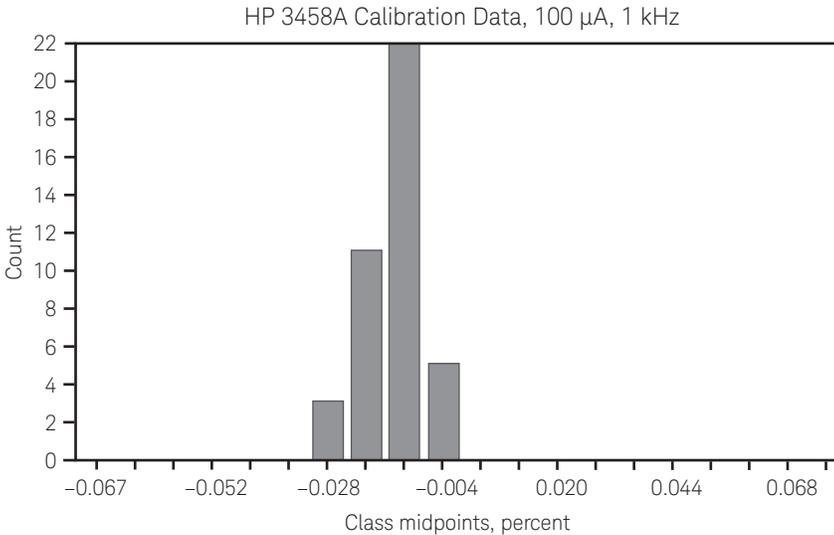


Figure 13.

## Measurement of Linearity Using a 10-Volt Josephson Junction Array

The extremely good linearity of the A/D converter of the 3458A is a key reason that it can offer such excellent performance. The only tool we have found capable of measuring that linearity is the 10-volt Josephson junction array. We have had a 10-volt array operational in the HP Loveland standards lab since November, 1988. The array chip was developed by and purchased from NIST, Boulder, Colorado. A detailed description of the Josephson junction array is beyond the scope of this paper. Reference 7 contains much of this detailed information.

Following is a very brief description of the operating characteristics of the array, how we use it, and a sample of results obtained on the 3458A A/D. In the use of the JJ array for linearity testing, its function can be described as that of a nearly ideal frequency-to-voltage converter. A single Josephson junction follows this basic equation:

$$V = \frac{nhf}{2e} = \frac{nf}{K_j}$$

where  $V$  = voltage of a selected "step" across the junction  $n$  = an integer,  $f$  = frequency of RF energy incident on the junction  $h$  = Planck's constant,  $e$  = charge of the electron and  $K_j$  = a defined constant representing  $2e/h$ .

To equate the volt as maintained by a Josephson junction to the SI unit, the quantity  $K_j$  must be chosen properly. As of January 1, 1990, the assigned value for  $K_j$  is 483597.9 GHz/V.

The 10-volt JJ array contains 18,992 junctions in series for DC voltage, and can produce extremely precise selectable DC voltage steps of either polarity. Using a frequency of about 70 GHz, the 10-volt array produces a DC voltage step approximately every 150  $\mu$ V, from -10 to +10 V. The precise value of each step is calculated and compared to the reading of the 3458A under test, which is also connected across the array. We have automated the linearity measurement process, and the system can measure the errors of a 3458A between -10 to +10 V in 0.5 V steps in about 20 minutes. A block diagram of our automated JJ array system is shown in Figure 14 and it is described further in [8] and [9].

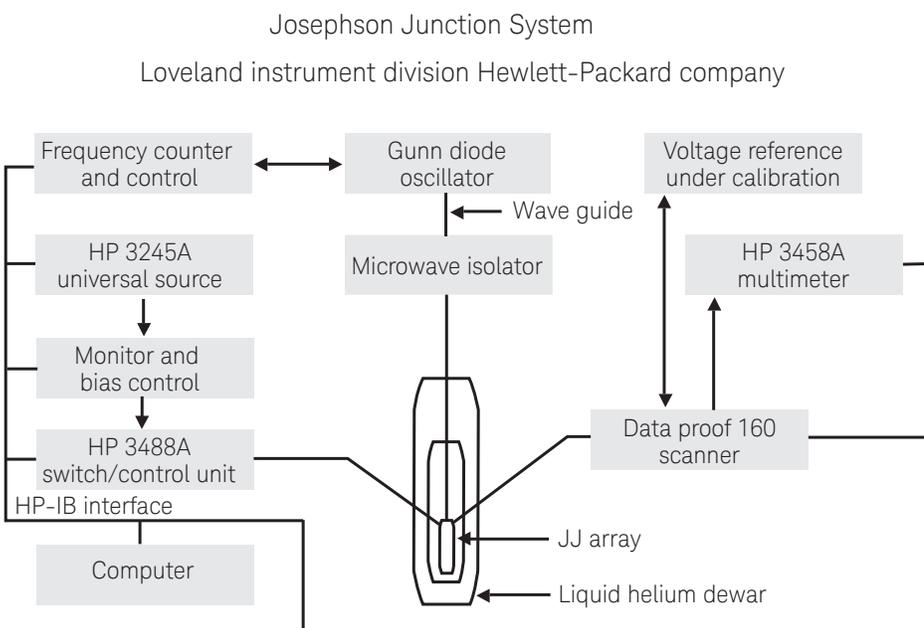


Figure 14.

## Measurement of Linearity Using a 10-Volt Josephson Junction Array (Continued)

Figure 15 shows the difference between 3458A reading and JJ array setting for two different DMVs. This plot does not reveal much about linearity. There is more than one accepted definition for linearity, but for purposes of this paper, it will be defined as the maximum deviation from a least squares straight line fit to the data represented by Figure 14.

Figure 16 shows the deviations from a fitted straight line. The maximum deviation necessary for proper operation of the 3458A is 0.1 ppm of full scale (1  $\mu\text{V}$ ). These two units are seen to easily meet that requirement. Many other HP 3458A's have been tested using the array and the results have been similar. By carefully characterizing some selected "special" instruments on a periodic basis, we are able to carry linearity testing to the production floor.

HP 3458A Linearity, Error Voltage  
10 V Range, #1499, 4/26/89

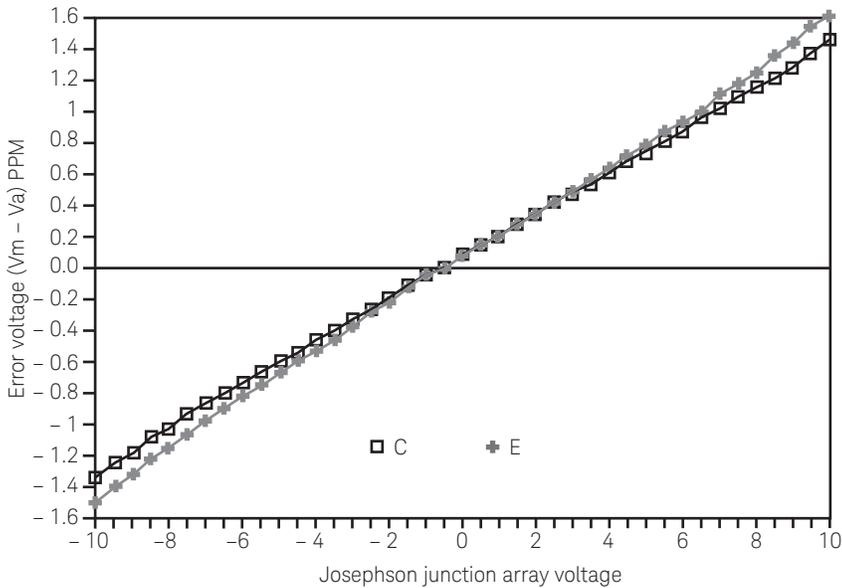


Figure 15.

HP 3458A Linearity, Offset from Least Square  
10 V Range, #1499, 4/26/89

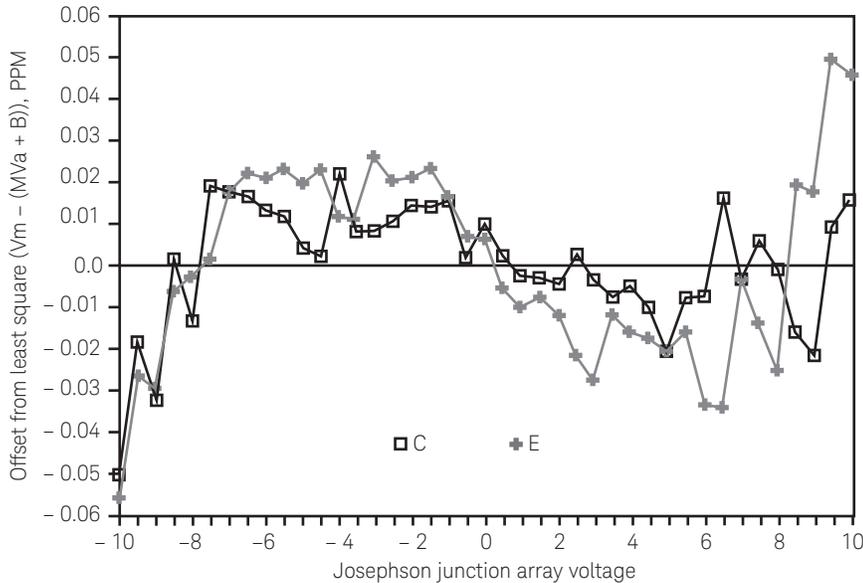


Figure 16.

## Measurement of Linearity Using a 10-Volt Josephson Junction Array (Continued)

### Summary

The arrival of a highly accurate DMM with automatic internal self-adjustment is a challenge to the metrologist, because evaluation of its performance requires him to carefully eliminate or compensate for more sources of error than ever before. The results that can be obtained with careful methods show excellent agreement with the DMM's measurements, enhancing confidence in both the methods and the DMM's performance. The methods presented in this paper have been demonstrated to be capable of verifying 24-hour specifications of the 3458A. These methods have been undergoing continuous improvement and will continue to be improved. Table 1 shows a sample set of data taken on a typical 3458A along with estimated uncertainties for each parameter. Data taken on a significant number of HP 3458As reveal distributions that are within 24-hour specifications for 87 separate parameters. A 10-volt Josephson Junction array is successfully being routinely used as a tool to verify linearity and also to provide a state-of-the-art DC voltage standard for evaluating the performance of the 3458A.

Data thus far accumulated on the performance of the HP 3458A indicate it should earn a place as a measurement tool that can be used to greatly enhance standards lab productivity and effectiveness.

Table 1.

<b>3458A test date</b>		
<b>Date: 01/30/89 Temp: 22.8 °C Rel Hum: 38%</b>		
<b>Temperature of 3458A: 37.2 °C Serial no.: 2823A00510 C#: 16014</b>		
<b>3458A test data (Incoming)</b>		
Nominal value	Error	Uncertainty
10 k ohm	0.9 PPM	0.5 PPM
10 V DC	1.3 PPM	1 PPM
<b>3458A test data (Outgoing)</b>		
Nominal value	Error	Uncertainty
0.1 V DC	0.0 PPM	2.0 PPM
-0.1 V DC	0.1 PPM	2.0 PPM
1 V DC	-0.4 PPM	1.0 PPM
-1 V DC	0.1 PPM	1.0 PPM
10 V DC	-0.2 PPM	0.5 PPM
-10 V DC	0.1 PPM	0.5 PPM
100 V DC	0.8 PPM	1.0 PPM
-100 V DC	1.4 PPM	1.0 PPM
1000 V DC	-2.3 PPM	2.0 PPM
-1000 V DC	-1.5 PPM	2.0 PPM
1 Ω	-28.2 PPM	1.0 PPM
10 Ω	-0.7 PPM	1.0 PPM
100 Ω	-0.5 PPM	1.0 PPM
1 kΩ	-0.2 PPM	1.0 PPM
10 kΩ	-0.5 PPM	1.0 PPM
100 kΩ	0.0 PPM	1.0 PPM
1 MΩ	-0.5 PPM	2.0 PPM
10 MΩ	-7.2 PPM	5.0 PPM
100 MΩ	-38.5 PPM	100.0 PPM

## Measurement of Linearity Using a 10-Volt Josephson Junction Array (Continued)

Table 1. Continued

3458A test data (Outgoing)		
Nominal value	Error	Uncertainty
100 nA DC	-1.6 PPM	35.0 PPM
-100 nA DC	4.0 PPM	35.0 PPM
1 $\mu$ A DC	0.7 PPM	22.0 PPM
-1 $\mu$ A DC	2.4 PPM	22.0 PPM
10 $\mu$ A DC	-0.7 PPM	10.0 PPM
-10 $\mu$ A DC	1.9 PPM	10.0 PPM
100 $\mu$ A DC	1.9 PPM	10.0 PPM
-100 $\mu$ A DC	0.2 PPM	10.0 PPM
1 mA DC	-1.2 PPM	5.0 PPM
-1 mA DC	0.8 PPM	5.0 PPM
10 mA DC	-1.03 PPM	5.0 PPM
-10 mA DC	2.2 PPM	5.0 PPM
100 mA DC	-0.4 PPM	5.0 PPM
-100 mA DC	9.0 PPM	5.0 PPM
1 A DC	-42.2 PPM	20.0 PPM
-1 A DC	-94.3 PPM	20.0 PPM
0.01 V 1 kHz	-0.010%	0.009%
0.01 V 20 kHz	-0.027%	0.009%
0.01 V 100 kHz	-0.269%	0.025%
0.01 V 300 kHz	-2.116%	0.210%
0.01 V 1 MHz	-0.116%	0.450%
0.1 V 1 kHz	-0.008%	0.006%
0.1 V 20 kHz	-0.010%	0.006%
0.1 V 100 kHz	-0.034%	0.012%
0.1 V 300 kHz	-0.168%	0.030%
0.1 V 1 MHz	-0.339%	0.100%
1 V 1 kHz	-0.002%	0.005%
1 V 20 kHz	-0.005%	0.005%
1 V 50 kHz	0.005%	0.005%
1 V 100 kHz	0.021%	0.008%
1 V 300 kHz	0.133%	0.015%
1 V 500 kHz	0.254%	0.050%
1 V 1 MHz	0.530%	0.100%
3 V 100 kHz	-0.006%	0.006%
10 V 10 Hz	0.002%	0.012%
10 V 20 Hz	0.001%	0.004%

## Measurement of Linearity Using a 10-Volt Josephson Junction Array (Continued)

Table 1. Continued

<b>3458A test data (Outgoing)</b>		
Nominal value	Error	Uncertainty
10 V 20 kHz	0.001%	0.004%
10 V 50 kHz	0.008%	0.004%
10 V 100 kHz	-0.001%	0.006%
10 V 300 kHz	-0.047%	0.015%
10 V 500 kHz	0.018%	0.040%
10 V 1 MHz	0.469%	0.080%
100 V 1 kHz	-0.007%	0.005%
100 V 20 kHz	-0.006%	0.005%
100 V 50 kHz	-0.002%	0.005%
100 V 100 kHz	-0.011%	0.008%
700 V 1 kHz	-0.002%	0.005%
0.01 V 4 MHz	-1.375%	0.300%
0.1 V 4 MHz	-1.500%	0.250%
0.1 V 8 MHz	0.192%	0.250%
0.1 V 10 MHz	7.745%	0.250%
1 V 4 MHz	1.097%	0.250%
1 V 8 MHz	0.145%	0.250%
1 V 10 MHz	1.882%	0.250%
3 V 2 MHz	-0.806%	0.200%
3 V 4 MHz	0.139%	0.250%
3 V 8 MHz	0.071%	0.250%
3 V 10 MHz	6.052%	0.250%
10 $\mu$ A 1 kHz	0.103%	0.080%
100 $\mu$ A 1 kHz	-0.018%	0.015%
1 mA 1 kHz	-0.010%	0.015%
10 mA 1 kHz	-0.008%	0.015%
100 mA 1 kHz	-0.010%	0.015%
1 A 1 kHz	-0.017%	0.015%

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